Like, Want, Would Like
¡No te confundas!

Want (Querer)
Do you want . . . ?
¿Quieres…?
Did you want…?
¿Querías…? O ¿Quisiste…?

Like (Gustar)
Do you like . . . ?
¿Te gusta…?
Did you like…?
¿Te gustaba…? / ¿Te gustó…?

Would like
(fórmula educada, amable para "querer") It means want. It does not mean like.
Would you like . . . ?
¿Querrías…? (petición amable). En español, a menudo decimos sólo "¿Quieres...? Pero en inglés, si pretendes ser amable, educada/o, pregunta con el "would".

Traduce los ejemplos:

(Gina has some candy. Al doesn't have any candy.)

Gina: Do you want some candy, Al? (friendly / casual = informal)
       Would you like some candy, Al? (polite = educado)

Al: No, thanks. (Al doesn't want any candy.)

(There's a good movie tonight. Bob hopes Cathy will go with him.)

Bob: There's a really good movie tonight. Would you like to see it with me?
       (Why does Bob use would like?)

Cathy: Yes, I'd like that very much. (Why does Cathy use would like?)

Other examples:

I like green tea. (I enjoy drinking green tea.)
I'd like green tea. (I want some green tea.)
I like visiting Internet chatrooms. (I enjoy that - a hobby.)
I'd like to visit Internet chatrooms. (I probably haven't visited Internet chatrooms, but this is something I want to do.)

Special Note:

Negative answers for polite "Would like . . .?" questions usually don't use "would like."
Instead, polite answers are usually "No, thank you" or something similar.